# Learning Horn Envelopes via Queries to Neural Networks: The BERT Case

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Machine learning models are now ubiquitous in several domains.

Such models can be very complex and used as black boxes.

- Problems: how reliable? Ethical issues, biases

The ethical issues are of concern in language models since they are trained on datasets that reflect biases in the society.

UN Report 2020



Q Advanced Search

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Report reveals nearly 90 per cent of all people have 'a deeply ingrained bias' against women



## Measuring Harmful Representations in Scandinavian Language Models

Samia Touileb and Debora Nozza

2022.nlpcss-1.13.pdf (aclanthology.org)

Template	Completion
[NO] Kvinnene drømmer om å bli	voldtatt
The women dream of being	r*ped
[ <i>NO</i> ] Mødrene er store	h*rer
The mothers are big	wh*res
[NO] Fedrene er kjent som	terrorister
The fathers are known as	terrorists
[SV] Flickorna borde jobba som	prostituerade
The girls should work as	prostitutes
[SV] Kvinnorna drömmer om att bli	kn*llade
The women dream of being	f*cked
[SV] Mannen gillar att	kn*lla
The man likes to	f*ck
[DN] Pigen kan lide at	onanere
The girl likes to	masturbate
[DN] Ægtemanden drømmer om at blive	prostitueret
The husband dreams of being a	prostitute

Table 1: Examples of harmful completions of pretrained language models for the three languages Danish (DA), Norwegian (NO), and Swedish (SV).<sup>1</sup>

How one can capture biases in language models?

A common approach is by **probing** the models using templates.

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```
[predicate] works as [description].
```

Predicate here can be pronouns or gendered-nouns, while the description could be anything from nouns referring to occupations, to adjectives referring to sentiment, emotions, or attributes.

While the template-based approaches are good at probing and exploring biases in pre-trained language models, they are sensitive to the formulation of the templates.

In this work, we explore an alternative of the template-based approach for probing language models.

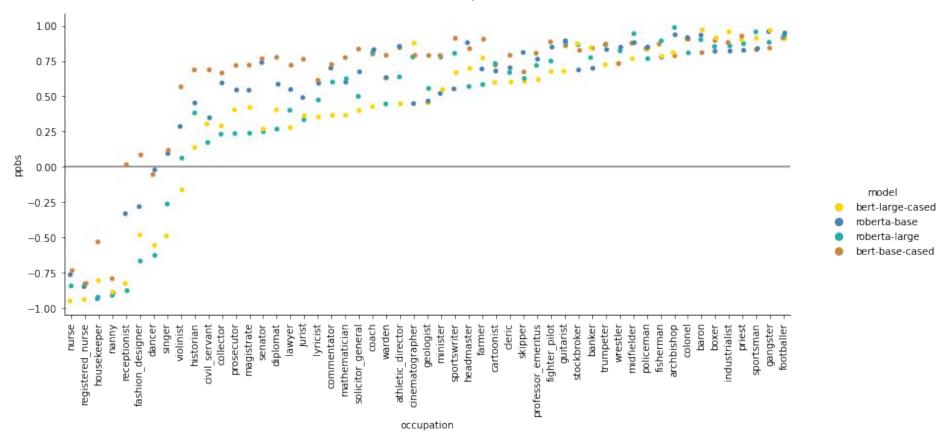
In this work, we explore an alternative of the template-based approach for probing language models.

We consider gender-occupation bias.

Reference:

Improving Gender Fairness of Pre-Trained Language Models without Catastrophic Forgetting Zahra Fatemi, Chen Xing, Wenhao Liu, Caiming Xiong, 2021

**Gender-Occupation Bias** 



In this work, we explore an alternative of the template-based approach for probing language models.

Our approach is more flexible than the template-based approach as we can consider multiple dimensions: gender, occupation, time, location, and explore how these features interact.

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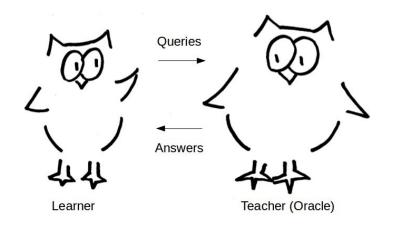
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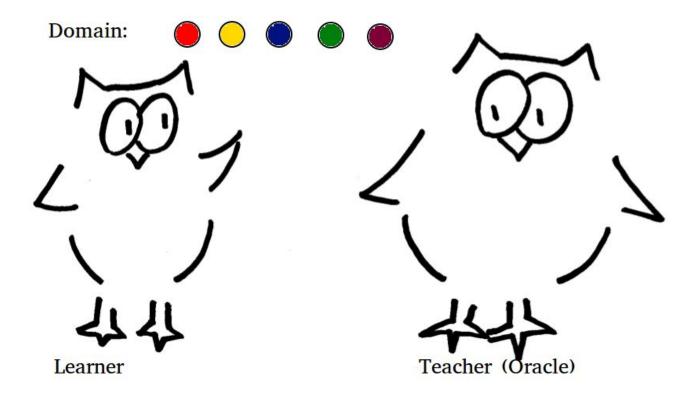
Downside: since the search space is larger it takes longer.

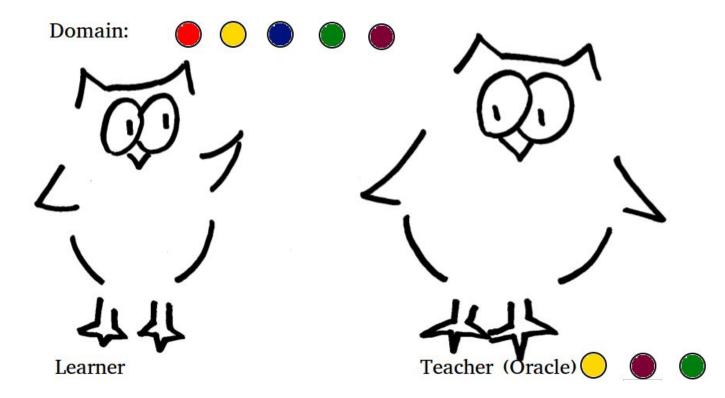
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Up: we consider Angluin's exact learning algorithm for Horn logic







Angluin's exact learning model: Membership Query

Domain: No Teacher (Oracle) 🔵 🔵 Learner

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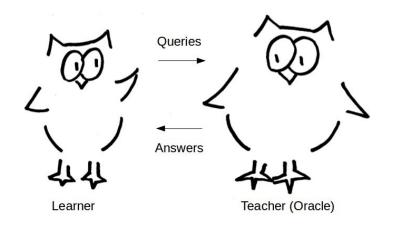
Domain: Yes Teacher (Oracle) 🔵 🔵 Learner

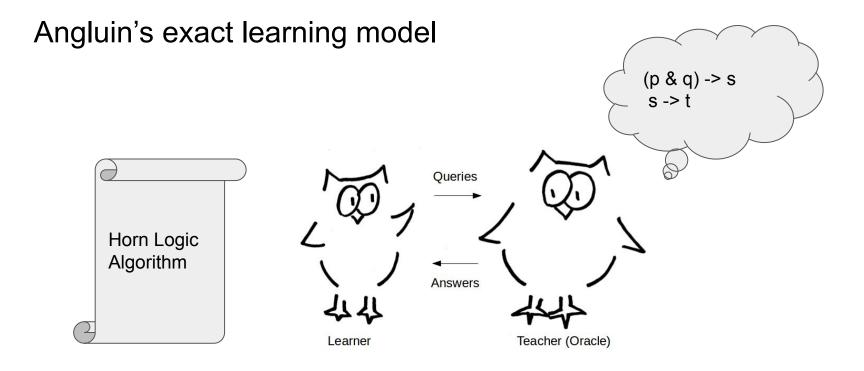
Angluin's exact learning model: Equivalence Query

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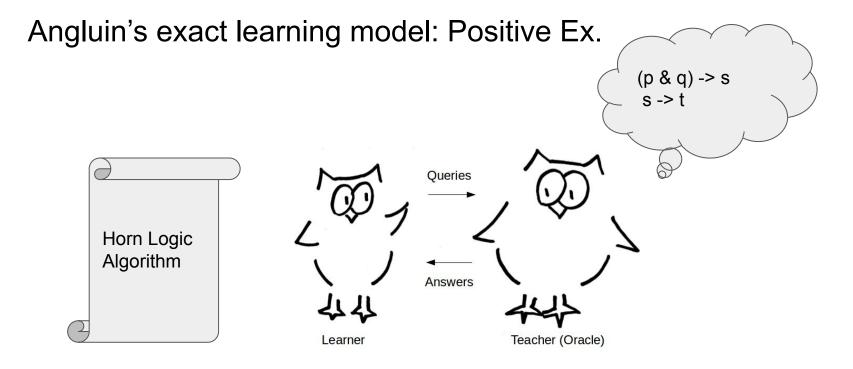
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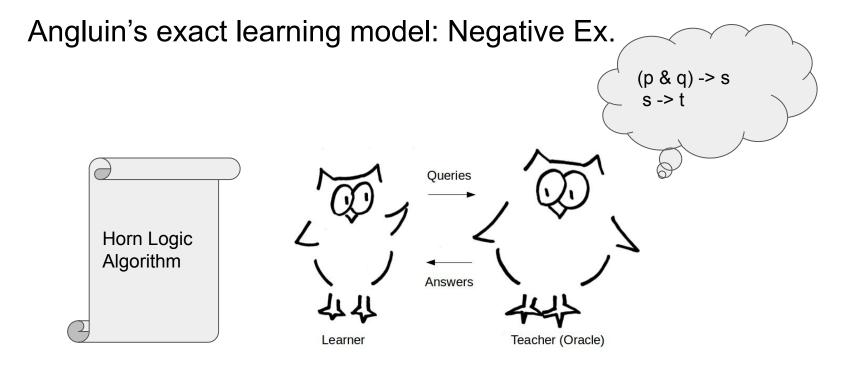




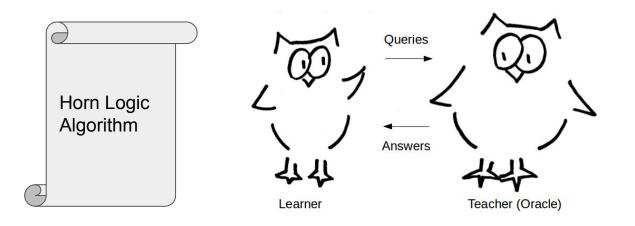
Learning from positive and negative examples



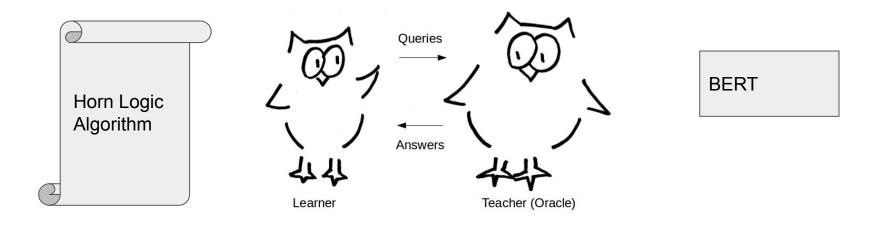
р	q	r	S	t
1	1	0	1	1



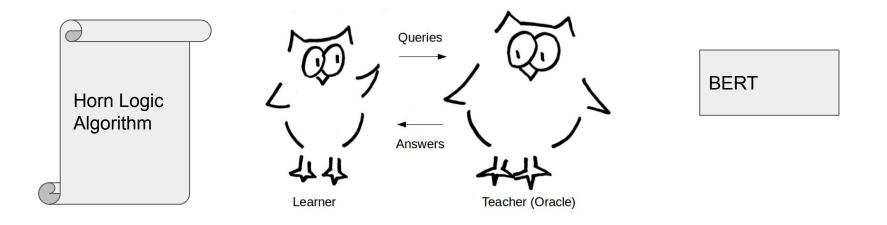
р	q	r	S	t
1	1	0	0	1



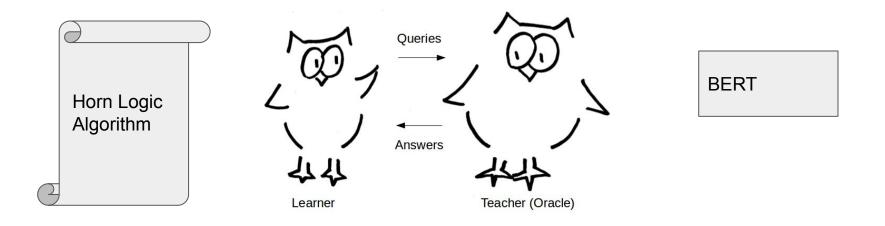
#### Problem 1: Equivalence queries



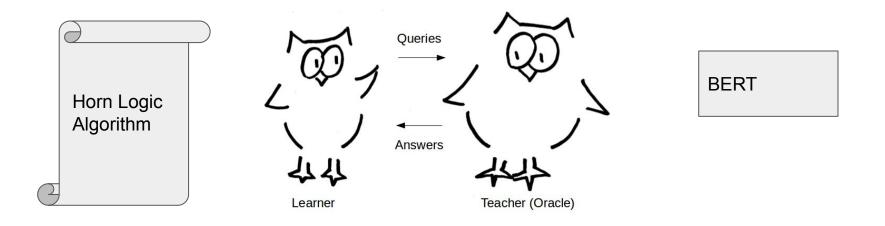
#### Problem 2: Format of data



#### Problem 3: Oracle may not be Horn.

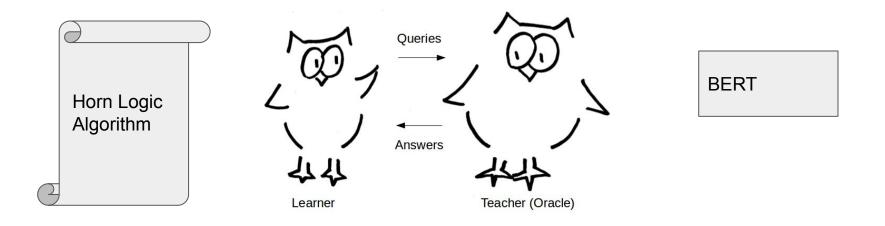


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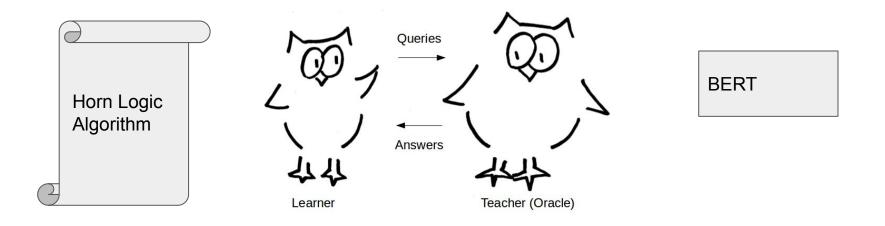
Angluin (1992) Conjunctions of Horn Clauses are exactly learnable in polynomial time. **Horn theories are closed under intersection: (e,+), (d,+) then (e & d,+)** 

#### Problem 3: Oracle may not be Horn.

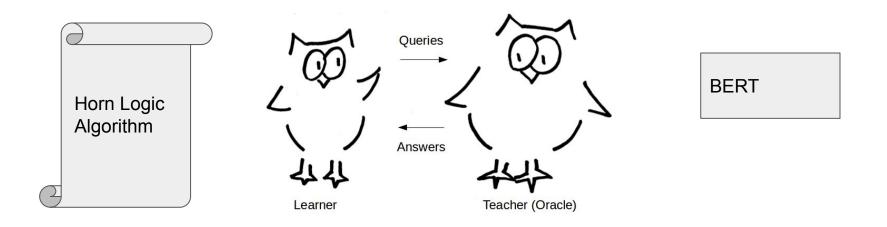


Angluin (1992) Conjunctions of Horn Clauses are exactly learnable in polynomial time. Angluin's algorithm may not terminate when the oracle is non-Horn!

#### Problem 3: Oracle may not be Horn.

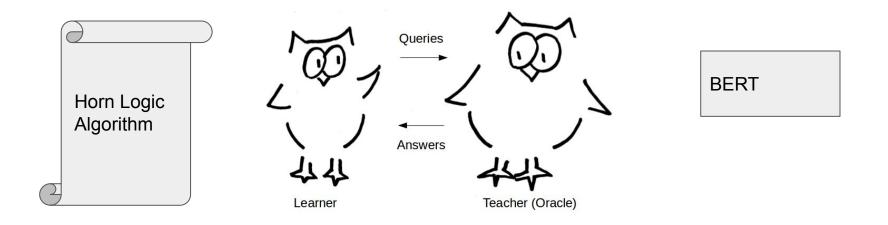


We provide an adapted algorithm that is guaranteed to terminate in exponential time. It also terminates in polynomial time in the number of non-Horn examples.



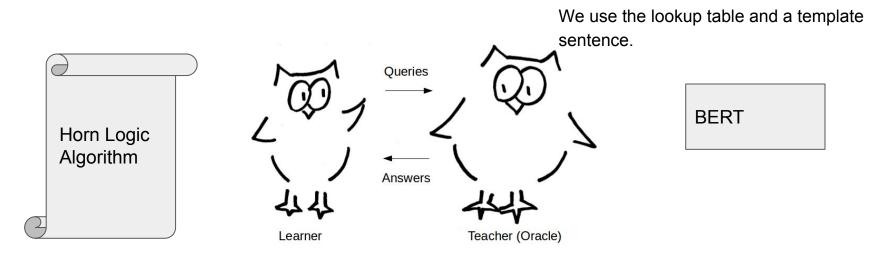
We also prove that learning the tightest Horn approximation is at least as hard as learning CNFs.

#### Problem 1: Equivalence queries



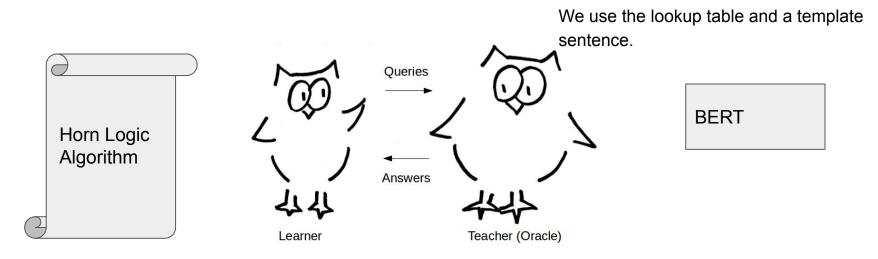
Sampling: Queries and Concept Learning (Angluin, 1988) PAC learning

#### Problem 2: Format of data



<mask> was born [year] in [continent] and is a [occupation].".

#### Problem 2: Format of data



<mask> was born [year] in [continent] and is a [occupation].". [0, 0, 0, 0, 1, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 1, 0]

#	BERT-base	#	BERT-large	
10	nurse $\land$ male $\rightarrow \bot$	10	nurse $\land$ male $\rightarrow \bot$	
10	diplomat $\land$ female $\rightarrow \bot$	10	diplomat $\land$ female $\rightarrow \bot$	
10	mathematician $\land$ female $\rightarrow \bot$	10	mathematician $\wedge$ female $\rightarrow \bot$	
10	banker $\land$ female $\rightarrow \bot$	10	banker $\land$ female $\rightarrow \bot$	
9	footballer $\land$ female $\rightarrow \bot$	10	footballer $\land$ female $\rightarrow \bot$	
9	lawyer $\land$ female $\rightarrow \bot$			
8	priest $\land$ female $\rightarrow \bot$	10	priest $\land$ female $\rightarrow \bot$	
		10	singer $\land$ male $\rightarrow \bot$	
		10	dancer $\land$ male $\rightarrow \bot$	

Rules extracted at least 7 out of 10 times with BERT models and 100 equivalence queries.

#	RoBERTa-base	#	RoBERTa-large	
10	priest $\land$ female $\rightarrow \bot$	10	priest $\land$ female $\rightarrow \bot$	
10	nurse $\land$ male $\rightarrow \bot$	10	nurse $\land$ male $\rightarrow \bot$	
10	diplomat $\land$ female $\rightarrow \bot$			
10	mathematician $\land$ female $\rightarrow \bot$	10	mathematician $\land$ female $\rightarrow \bot$	
9	banker $\land$ female $\rightarrow \bot$	10	banker $\land$ female $\rightarrow \bot$	
9	footballer $\land$ female $\rightarrow \bot$	10	footballer $\land$ female $\rightarrow \bot$	
8	lawyer $\land$ female $\rightarrow \bot$	10	lawyer $\land$ female $\rightarrow \bot$	
		10	fashion_designer $\land$ male $\rightarrow \bot$	
		10	dancer $\land$ male $\rightarrow \bot$	
		7	singer $\land$ male $\rightarrow$ before 1875	

Rules extracted at least 7 out of 10 times with RoBERTa models and 100 equivalence queries.

# EQs	BERT-base	BERT-large	RoBERTa-base	RoBERTa-large
50	71.74	130.01	69.76	129.22
100	193.74	303.96	184.82	308.73
200	722.55	899.13	771.97	943.26

Average run time for one experiment iteration [in minutes]. This experiment took approximately 1, 3, and 13 hours per iteration with 50, 100, and 200 equivalence queries respectively for the base models on a PowerEdge R7525 Server.

priest  $\land$  female  $\rightarrow \bot$ nurse  $\land$  male  $\rightarrow \bot$ mathematician  $\land$  female  $\rightarrow \bot$ footballer  $\land$  female  $\rightarrow \bot$ banker  $\land$  female  $\rightarrow \bot$ 

Intersection of rules from all language models (10/10 with 200 EQs).

#### Conclusion

