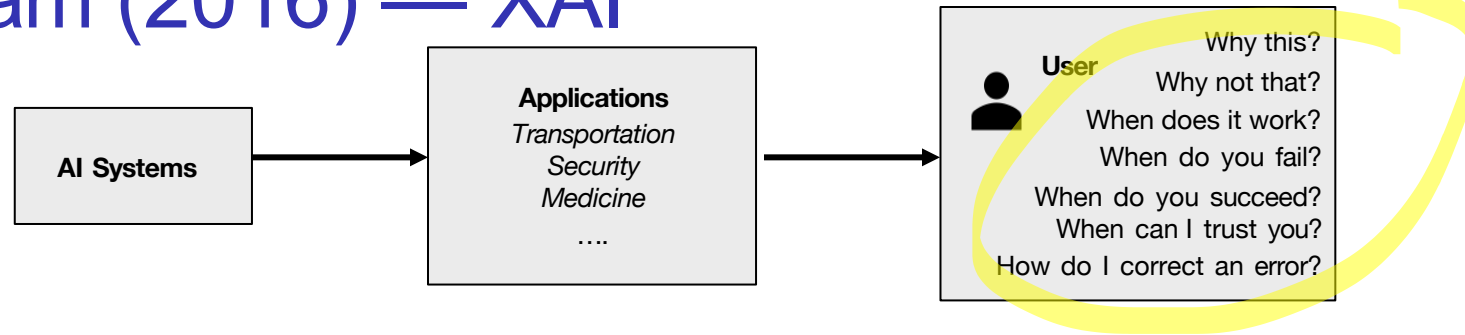


# Model Reconciliation & Its Applications in Explainable AI

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# Explainable AI

## DARPA Program (2016) — XAI



Focus on machine learning systems — **proposed theme:**

- ❑ Producing explainable models (learning explanatory semantics: features, representations, structures, causal models, etc.) → [Producing explainable models, computing models]
- ❑ Designing explanation interface → [HCI]
- ❑ Understanding the psychological requirements for effective explanations → [Psychology]

<https://www.darpa.mil/attachments/DARPA-BAA-16-53.pdf>

# This Talk

- Explainable planning and model reconciliation
- Model reconciliation problem (MRP) under the lens of logic
- Solving MRP and applications of MRP

An **explanation** is a set of statements usually constructed to **describe** a set of facts which clarifies the **causes**, **context**, and **consequences** of those facts. This description may establish rules or laws and may clarify the existing **rules** or **laws** in relation to any objects, or phenomena examined.

*Source: Introduction to Logic. Jess Drake (2018).*

# Explainable Planning

- ❑ Explainable AI **in planning**
- ❑ Relevant to xAI but also different from xAI
  - ❑ human and intelligent robots working together
  - ❑ white box vs. black box
- ❑ Different facets – who explains to whom
- ❑ Lot of interest and activities (e.g., xAIP workshop series: <https://xaip.mybluemix.net>)
- ❑ References: many in <https://explainableplanning.com>

# Dimensions of Explainable Planning

- Planning model

- classical planning
- probabilistic planning
- MDP/POMDP
- ...

- Knowledge of the explainer (robot)

- both models
- only its internal model

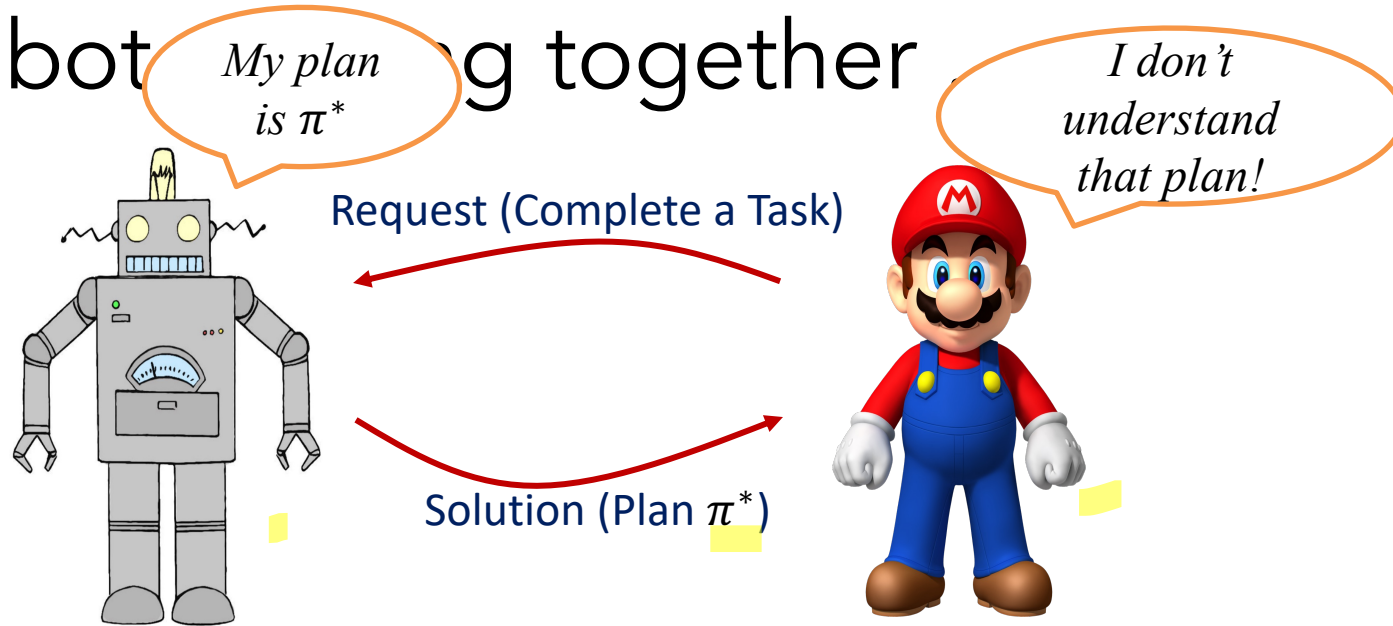
☞ **one shot explanation**

☞ **dialog for explanation**



# Model Reconciliation in xAIP

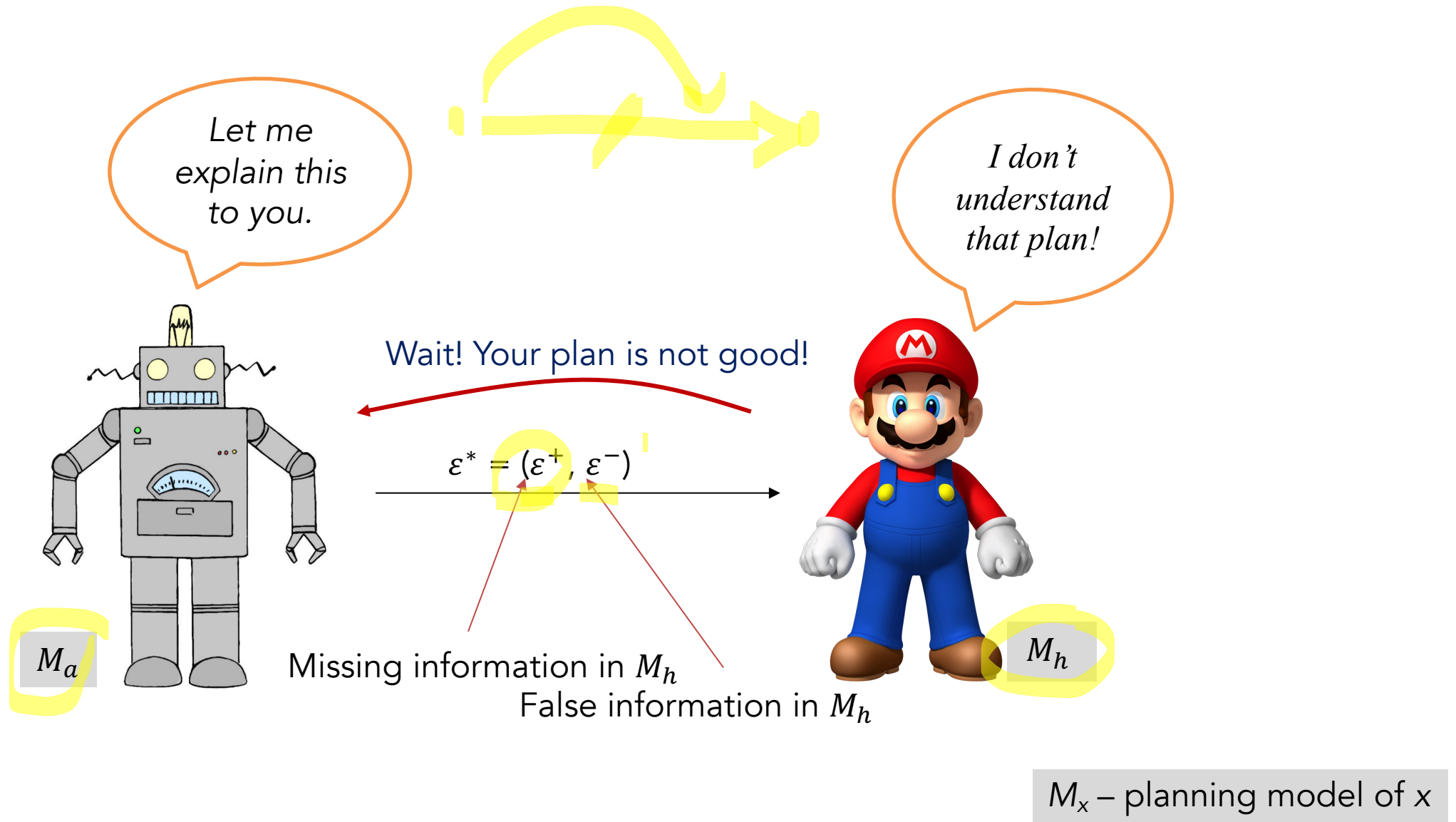
Human and robot working together



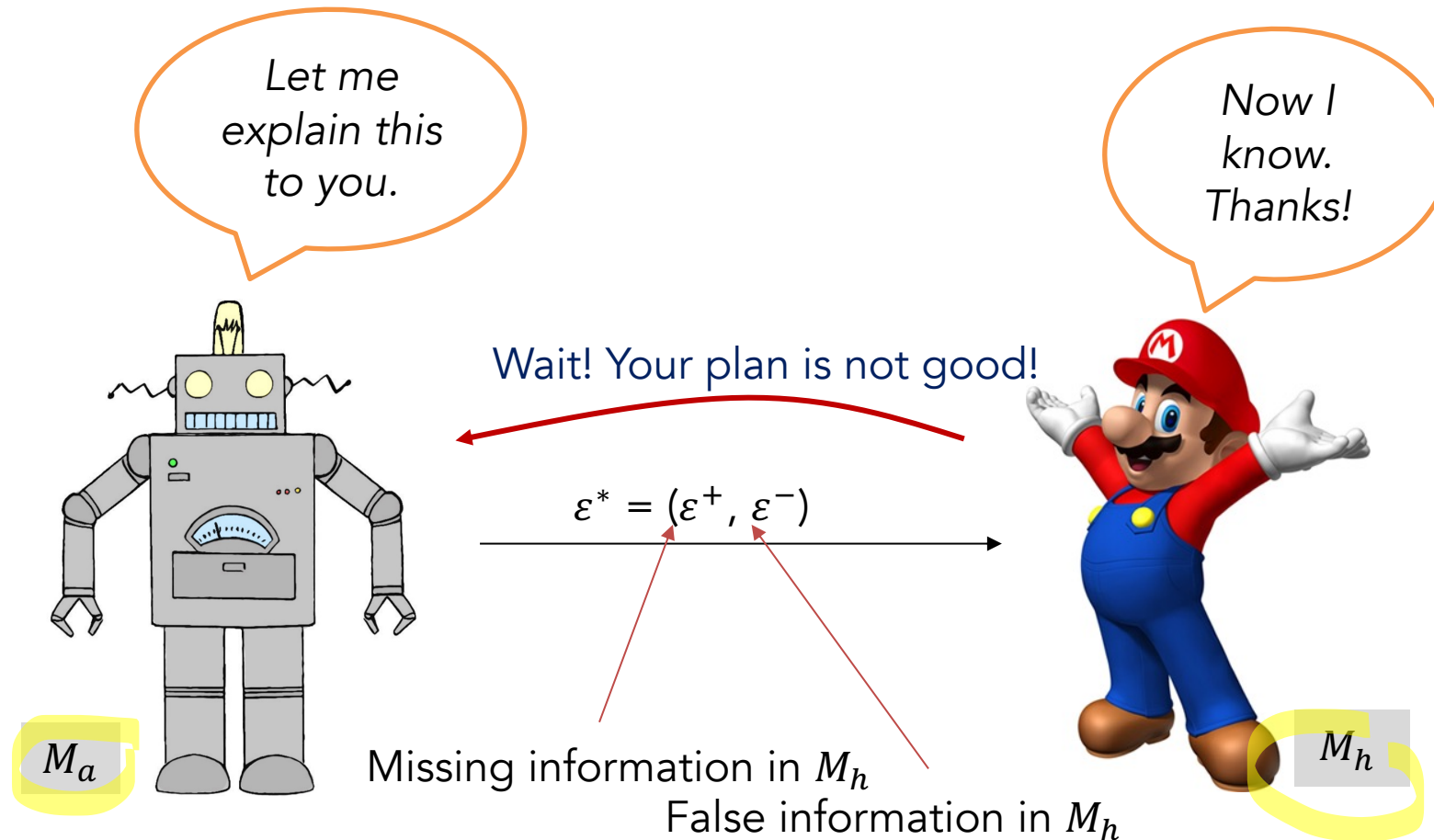
- ❑ Human asks robot to accomplish a task and how the robot would complete it.
- ❑ Robot presents a plan.
- ❑ Human might have different plan  $\pi'$  *that is better* than the proposed plan.
- ❑ Explanation is needed!

Model reconciliation as an approach to solving xAIP

# Model Reconciliation in xAIP



# Model Reconciliation in xAIP



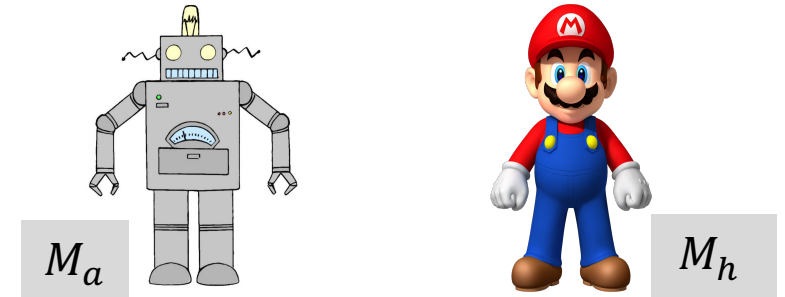
After reconciliation –  $M_h \setminus \epsilon^- \cup \epsilon^+$   
accepts the plan  $\pi^*$  of robot as valid

$M_x$  – planning model of  $x$



# Formalization

- Two agents (robot and human) with two planning problems  $M_a$  and  $M_h$



- Robot informs human about an optimal solution  $\pi^*$  for a goal  $G$  (written as  $M_a \models \pi^*$  and  $M_h \not\models \pi^*$ )
- Compute  $\varepsilon = (\varepsilon^+, \varepsilon^-)$  such that  $M_h \setminus \varepsilon^- \cup \varepsilon^+ \models \pi^*$

$M \models \pi$ :  $\pi$  is a plan in the model  $M$

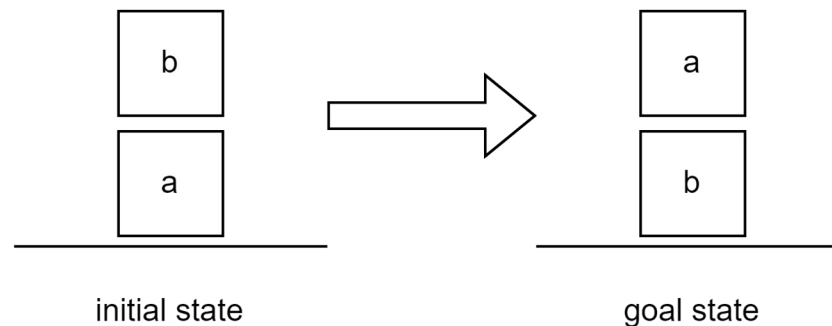
# Example – Block World Problem

## Model of Robot

- $stack(x,y)$ 
  - Precondition:  $holding(x), clear(y)$
  - Postcondition:  $handempty, on(x,y), \neg clear(y), clear(x)$
- $unstack(x,y)$ 
  - Precondition:  $handempty, on(x,y), clear(x)$
  - Postcondition:  $holding(x), clear(y), \neg clear(x)$
- ...

Optimal Plan:

1.  $unstack(b,a)$
2.  $putdown(b)$
3.  $pickup(a)$
4.  $stack(a,b)$



## Model of Human (missing precondition)

- $stack(x,y)$ 
  - Precondition:  ~~$holding(x)$~~ ,  $clear(y)$
  - Postcondition:  $handempty, on(x,y), \neg clear(y), clear(x)$
- Other actions are as in the model of the robot.

Optimal Plan:  
1.  $stack(a,b)$

**Explanation: missing  $holding(x)$  as a precondition of  $stack(x,y)$**

# Research in Model Reconciliation in xAIP

- ❑ Computing minimal explanations
- ❑ One-shot: *the agent (robot) who computes an explanation knows both domain descriptions*
  - ❑ Specialized algorithms
  - ❑ Answer set programming-based algorithm
- ❑ Dialog (limited effort): *the agent (robot) who computes an explanation does not know the human domain description* – more realistic – later ...

# Computing Explanations for xAIP

Input:  $M_a$ ,  $M_h$ , and  $\pi^*$  such that  $M_a \models \pi^*$  and  $M_h \not\models \pi^*$

Output: An explanation  $(\varepsilon^+, \varepsilon^-)$  for  $(M_a, M_h, \pi^*)$

repeat

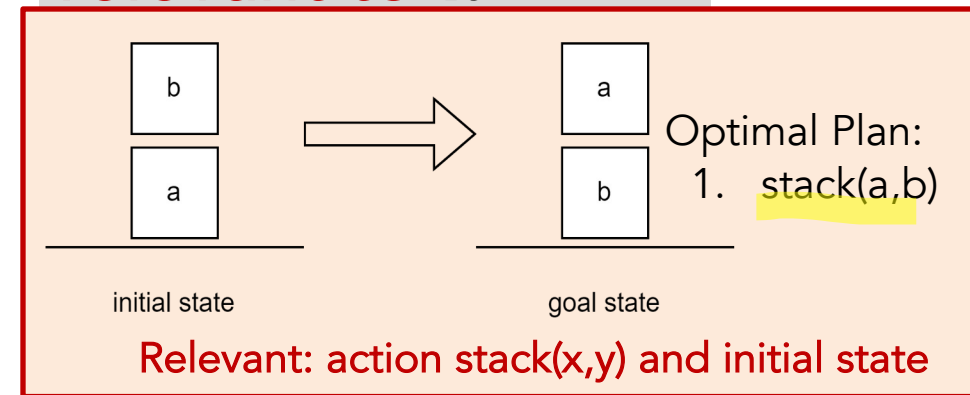
non-deterministically select a potential  $(\varepsilon^+, \varepsilon^-)$

if  $M_h \setminus \varepsilon^- \cup \varepsilon^+ \models \pi^*$

then return  $(\varepsilon^+, \varepsilon^-)$

until all possible explanations are considered

how to select?  
relevant to  $\pi^*$



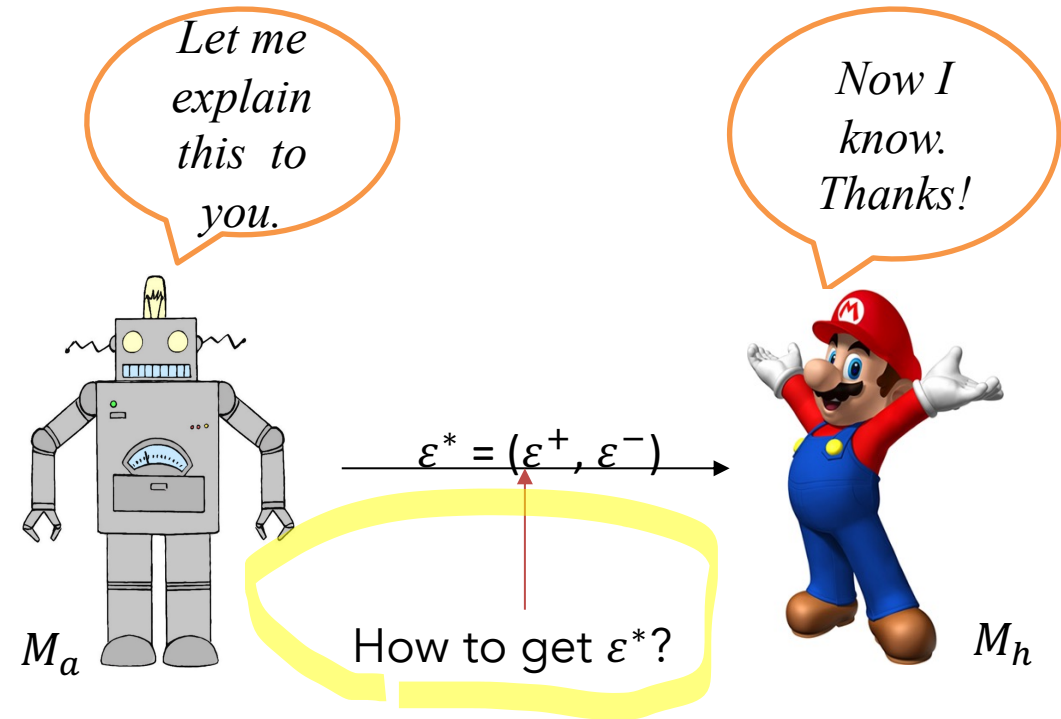
## Note

- ❑ Only for one-shot explanation (knowledge of both  $M_a$  and  $M_h$ )
- ❑ ASP implementation comparable with state of the art (Nguyen et al. - KR 2020)
- ❑ SAT implementation (Vasileiou et al. - JAIR 2022, AAAI 2021)

# From One-Shot Explanation to Dialog

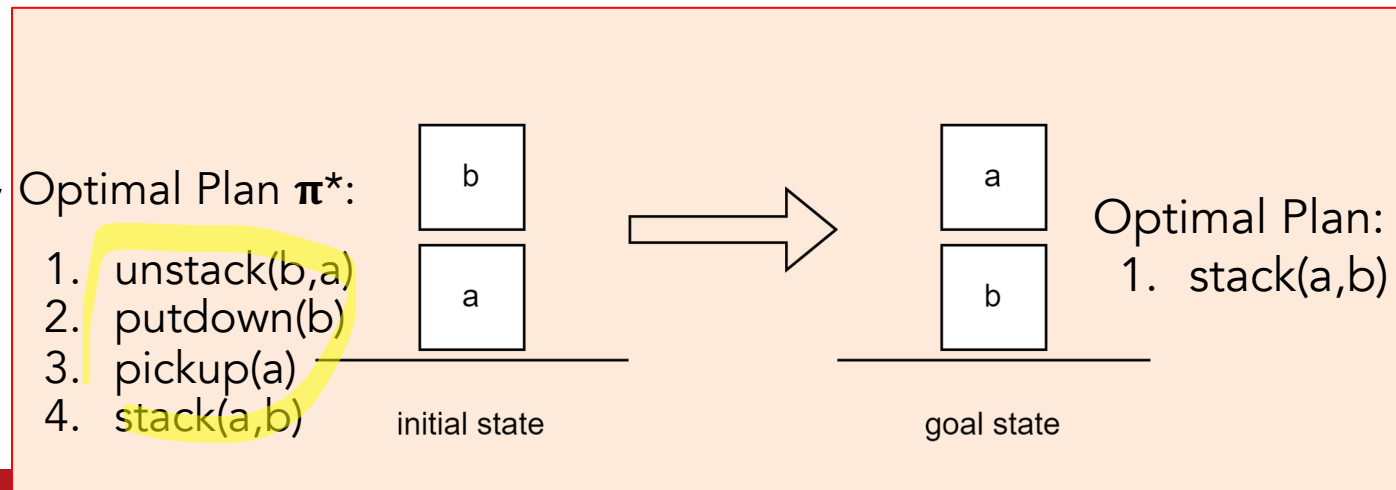
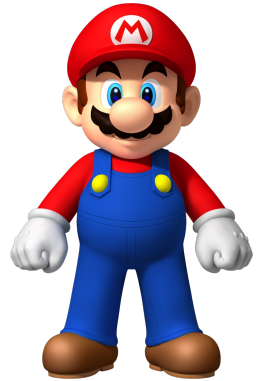
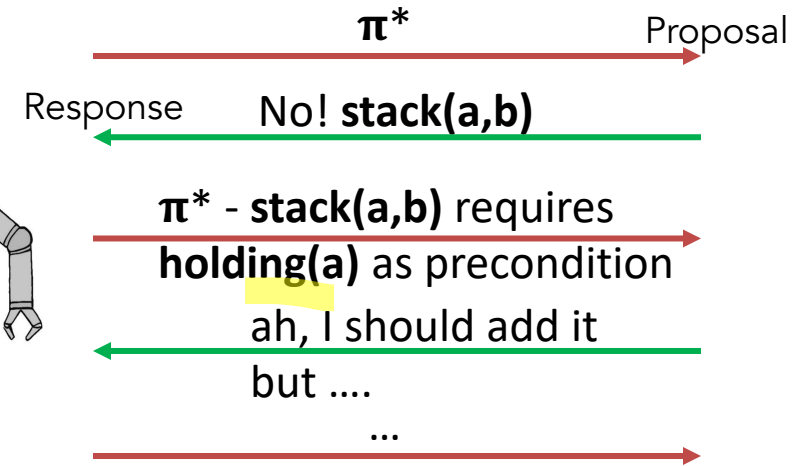
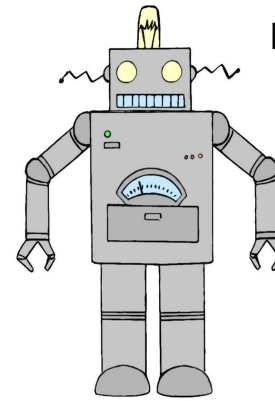
□ What if *the agent (robot) who computes a solution does not know the domain description of the human?*

□ Need to compute explanations by talking to each other, perhaps through multiple exchanges



# From One-Shot Explanation to Dialog

- ❑ Robot informs human of optimal plan  $\pi^*$  and potential explanation  $\epsilon$
- ❑ Human reveals issues about  $\pi^*$  and  $\epsilon$ 
  - ❑ the plan is not optimal
  - ❑ some action in  $\pi^*$  cannot be executed in the updated model
  - ❑ Some goal cannot be achieved
  - ❑ ...
- ❑ Robot receives the responses, identifies the issues, sends updated explanation



# From One-Shot Explanation to Dialog

- ❑ Robot sends human optimal plan  $\pi^*$  and  $\epsilon$  (initially,  $\epsilon = \emptyset$ )
- ❑ Human update  $M_h$  with  $\epsilon$ 
  - ❑ the plan is not my solution,  $\pi'$  is better because
    - ☞ the plan  $\pi^*$  is not executable or does not achieve the goal
    - ☞ some action's precondition is relaxed or
    - ☞ some action's postcondition becomes true when it is not supposed to
  - ❑ some action cannot be executed
  - ❑ some goal cannot be achievedsend the information to robot
- ❑ Robot identifying potential problems in human's response
  - => create new  $\epsilon$

# Explanation and Proposal

- Given a model  $M = (I, G, D)$  – as a set of atoms representing a planning problem
  - $add(M) = \{add(x) \mid x \in M\}$
  - $remove(M) = \{delete(x) \mid x \text{ is an atom representing an element of a planning model}\}$
- $\varepsilon \subseteq add(M) \cup remove(M)$  is an **explanation** if there is no  $x$  such that  $add(x) \in \varepsilon$  and  $remove(x) \in \varepsilon$  ;
- $(\pi, \varepsilon)$  is a **proposal** w.r.t.  $M$  where  $\pi$  is an optimal solution for  $M$  and  $\varepsilon$  is an explanation



# Response

$(\boldsymbol{\pi}, \boldsymbol{\varepsilon})$  is a proposal w.r.t.  $M_a$

$$M_h \otimes \boldsymbol{\varepsilon} = M_h \setminus \{x \mid \text{remove}(x) \in \boldsymbol{\varepsilon}\} \cup \{x \mid \text{add}(x) \in \boldsymbol{\varepsilon}\}$$

A **response** for  $(\boldsymbol{\pi}, \boldsymbol{\varepsilon})$  w.r.t.  $M_h$

- *acceptable*:  $(\top, \top)$  if  $M_h \otimes \boldsymbol{\varepsilon}$  has  $\boldsymbol{\pi}$  as an optimal plan
- *non-optimal*:  $(\boldsymbol{\pi}', \top)$  if  $M_h \otimes \boldsymbol{\varepsilon}$  has  $\boldsymbol{\pi}'$  as a “better” plan than  $\boldsymbol{\pi}$
- *redundant information*:  $(\perp, \boldsymbol{\varepsilon}')$  where  $\boldsymbol{\varepsilon}' = (\text{add}(M_h) \cap \boldsymbol{\varepsilon}) \cup \{\text{remove}(x) \mid x \notin M_h \text{ and } \text{remove}(x) \in \boldsymbol{\varepsilon}\}$
- *not executable*:  $(*, \boldsymbol{\omega})$  where  $\boldsymbol{\omega}$  encodes the information why  $\boldsymbol{\pi}$  cannot be executed in  $M_h \otimes \boldsymbol{\varepsilon}$

# Dialog

Given  $(M_a, M_h, \pi^*)$  a **dialogue** between robot and human is a sequence of rounds  $(x_i, y_i)$  where

- each  $x_i = (\pi^*, \epsilon)$  is a proposal w.r.t.  $M_a$
- each  $y_i$  is a response for  $x_i$  w.r.t.  $M_h$

A dialog is **successful** if it is finite and the last response is an acceptable response (for both parties)

## Note

- Clear separation of two parties (explainer and explainee)
- ASP implementation (*Ho & Son - ICLP 2022*)
- Argumentation based formalization (*Vasileiou et al. - upcoming*)

# Model Reconciliation Problem (MRP)

**Representation:** knowledge bases of robot and human are represented by logical theories  $KB_a$  and  $KB_h$  in some logic  $L$ , respectively.

$\models^c$  and  $\models^s$  — credulous and skeptical entailment relationship between theories and formulae in  $L$ , respectively.

**Exchange:** question about the truth value of formulas over literals occurring in  $KB_a$  and  $KB_h$ .

**Answer:** suggested modification to the knowledge base of the questioner.

# Model Reconciliation Problem (MRP)

**Representation:** knowledge bases of robot and human are represented by logical theories  $KB_a$  and  $KB_h$  in some logic  $L$ , respectively.

$\models^c$  and  $\models^s$  — credulous and skeptical entailment relationship between theories and formulae in  $L$ , respectively.

**Two types of questions (exchanges):**

**Entailment MRP** (e-MRP): why does  $KB_a \models^c \phi$  and  $KB_h \models^s \neg\phi$ ?

Determining  $\varepsilon^+ \subseteq KB_a$  and  $\varepsilon^- \subseteq KB_h$  such that  $(KB_h \setminus \varepsilon^-) \cup \varepsilon^+ \models^c \phi$ .

**non-Entailment MRP** (n-MRP): why does  $KB_a \models^s \phi$  and  $KB_h \models^c \neg\phi$ ?

Determining  $\varepsilon^+ \subseteq KB_a$  and  $\varepsilon^- \subseteq KB_h$  such that  $(KB_h \setminus \varepsilon^-) \cup \varepsilon^+ \models^s \phi$ .

**Compute a solution  $(\varepsilon^+, \varepsilon^-)$  of a MRP  $(KB_a, KB_h, \phi)$ .**

# Connection to xAIP

$KB_{a/h}$  = collection of formulae encoding the transition function for reasoning about effects of actions  
**plus** the description of the initial state  
**plus** the description of the goal Well-known SAT or ASP encoding

$KB_a \models^c \phi$  (goal)  $\sim$  extracted plan for  $\phi$  exists  
in SAT/ASP – length is a parameter of KB

- $\alpha$  an optimal plan for the robot and not the human
- e-MRP:  $KB_a \models^c \phi$  but  $KB_h \not\models^s \phi$

# Characterizing Explanations

Given  $(KB_a, KB_h, \phi)$  and an explanation  $(\varepsilon^+, \varepsilon^-)$

- $(\varepsilon^+, \varepsilon^-)$  is *optimal* if there exists no explanation  $(\lambda^+, \lambda^-)$  such that  $\lambda^+ \cup \lambda^- \subset \varepsilon^+ \cup \varepsilon^-$ . (always exists)
- $(\varepsilon^+, \varepsilon^-)$  is  *$\pi$ -restrictive* for  $\pi \subseteq KB_a$  if  $\varepsilon^+ \subseteq \pi$ . (existence depends on  $\pi$ )
  - *minimally-restrictive* if there exists no explanation  $(\lambda^+, \lambda^-)$  such that  $\lambda^+ \subset \varepsilon^+$ . (always exists)
- $(\varepsilon^+, \varepsilon^-)$  is  *$\pi$ -preserving* for  $\pi \subseteq KB_h$  if  $\pi \cap \varepsilon^- = \emptyset$ ; (existence depends on  $\pi$ )
  - *maximally-preserving* if there exists no explanation  $(\lambda^+, \lambda^-)$  such that  $\lambda^- \subset \varepsilon^-$ . (always exists)

# Cost-Based Characterization

Cost function  $C: KB_a \cup KB_h \rightarrow R^{\geq 0}$  (elements in  $KB_a$  and  $KB_h$  are representation unit).

$$C(\varepsilon^+, \varepsilon^-) \stackrel{def}{=} \sum_{r \in \varepsilon^+ \cup \varepsilon^-} C(r)$$

$(\varepsilon^+, \varepsilon^-)$  **cost optimal** w.r.t.  $C$  if  $C(\varepsilon^+, \varepsilon^-)$  is minimal among all explanation.

Given  $C$  of  $(KB_a, KB_h, \phi)$

□ *uniform* if  $C(r) = c$  (constant,  $> 0$ ) for  $r \in KB_a \cup KB_h$

cost-optimal explanation w.r.t.  $C$  is optimal

□ *agent-biased* if  $C(r) = c$  for  $r \in KB_a$  and  $C(r) = 0$  for  $r \in KB_h$ .

cost-optimal explanation w.r.t.  $C$  is minimally-restrictive

□ *human-biased* if  $C(r) = 0$  for  $r \in KB_a$  and  $C(r) = c$  for  $r \in KB_h$ .

cost-optimal explanation w.r.t.  $C$  is maximally-preserving

# Computing Explanation: What is Needed?

- Given: Logic  $L$ , formula  $\phi = \phi^+ \wedge \phi^-$ ,  $KB_a$  and  $KB_h$   
( $KB_a \models^c \phi^+$  and  $KB_a \models^s \phi^-$ ) and ( $KB_h \not\models^c \phi^+$  or  $KB_h \not\models^s \phi^-$ )
- Compute  $(\varepsilon^+, \varepsilon^-)$  so that  $KB_h \setminus \varepsilon^- \cup \varepsilon^+ \models^c \phi^+$  and  $KB_h \setminus \varepsilon^- \cup \varepsilon^+ \models^s \phi^-$
- How to
  - $\models^c$  and  $\models^s$ ? (logic dependent)
  - $KB_h \setminus \varepsilon^- \cup \varepsilon^+$  (updating a logical theory, logic and structural dependent)

**Propositional logic:**  $\models^c$  (SAT) and  $\models^s$  (UNSAT)

**ASP:**  $\models^c$  (one answer set, brave) and  $\models^s$  (all answer sets, skeptical)

**Argumentation Framework:**  $\models^c$  (credulous) and  $\models^s$  (skeptical)



# Computing Explanation: What is Needed?

- Given: Logic  $L$ , formula  $\phi = \phi^+ \wedge \phi^-$ ,  $KB_a$  and  $KB_h$   
( $KB_a \models^c \phi^+$  and  $KB_a \models^s \phi^-$ ) and ( $KB_h \not\models^c \phi^+$  or  $KB_h \not\models^s \phi^-$ )
- Compute  $(\varepsilon^+, \varepsilon^-)$  so that  $KB_h \setminus \varepsilon^- \cup \varepsilon^+ \models^c \phi^+$  and  $KB_h \setminus \varepsilon^- \cup \varepsilon^+ \models^s \phi^-$
- How to
  - $\models^c$  and  $\models^s$ ? (logic dependent)
  - $KB_h \setminus \varepsilon^- \cup \varepsilon^+$  (updating a logical theory, logic and structural dependent)

Propositional logic: ?

ASP: ?

Argumentation Framework: ?

Updating operator  $KB \otimes (\varepsilon^+, \varepsilon^-)$

# Computing Explanation

**Input:** Logic  $L$ , formula  $\phi = \phi^+ \wedge \phi^-$ ,  $KB_a$  and  $KB_h$   
( $KB_a \models^c \phi^+$  and  $KB_a \models^s \phi^-$ ) and ( $KB_h \not\models^c \phi^+$  or  $KB_h \not\models^s \phi^-$ )

**Output:** A solution for  $(KB_a, KB_h, \phi)$

**repeat**

non-deterministically select a potential  $(\varepsilon^+, \varepsilon^-)$

if  $KB_h \not\models^c \varepsilon^- \cup \varepsilon^+ \models^c \phi^+$  and  $KB_h \not\models^s \varepsilon^- \cup \varepsilon^+ \models^s \phi^-$

then return  $(\varepsilon^+, \varepsilon^-)$

**until** all possible explanations are considered

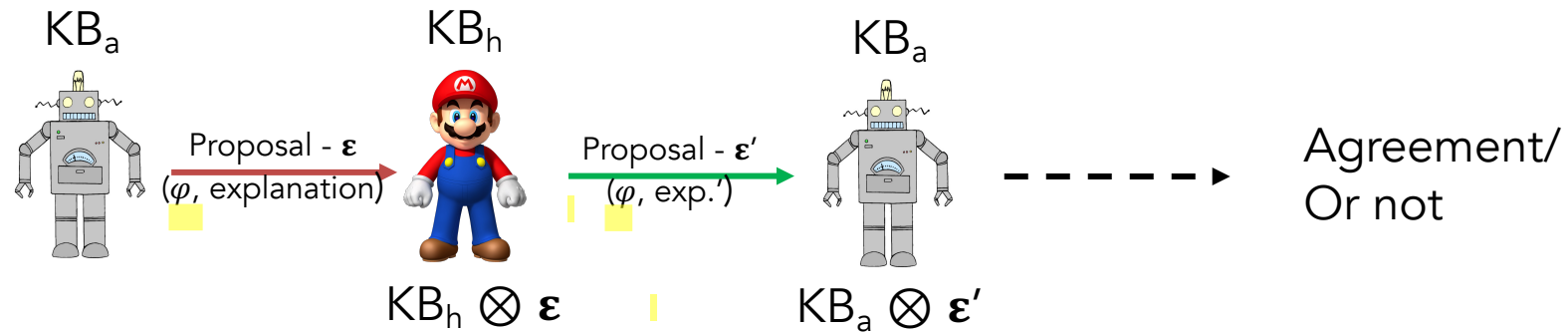
□ Only for one-shot situation (knowledge of both  $KB_a$  and  $KB_h$ )

# Dialog for Model Reconciliation

Explanation – sub-theory

Proposal – ( $\varphi$ , explanation)

Dialog – sequence of proposal exchanges



Is model reconciliation the same as dialog/negotiation?

# Towards a full ASP Implementation of MRP

- Propositional logic program  $\Pi$ , rule of the form
$$r : \quad a_0 \leftarrow a_1, \dots, a_m, \text{not } a_{m+1}, \dots, \text{not } a_n$$
$$\text{head}(r): a_0, \text{pos}(r): \{a_1, \dots, a_m\}, \text{neg}(r): \{a_{m+1}, \dots, a_n\}$$
- $\Pi^S$ : reduction of  $\Pi$  with respect to a set of atoms  $S$ .
- $T_\Pi$ : immediate consequence operator for positive programs.
- $S = \text{lfp}(T_\Pi^S)$ : answer set.
- $S$  is a **justification** for  $q$  with respect to an answer set  $I$  if  $S \subseteq \Pi$  such that  $\text{head}(r) \in I$  and  $I \models \text{body}(r)$  for  $r \in S$  and  $q \in \text{lfp}(T_\Pi^S)$ .

What is available?

- $\Pi \models^c a$ :  $a$  in some answer set of  $\Pi$
- $\Pi \models^s a$ :  $a$  in all answer sets of  $\Pi$
- $\varepsilon$  – rules and facts

What is missing?

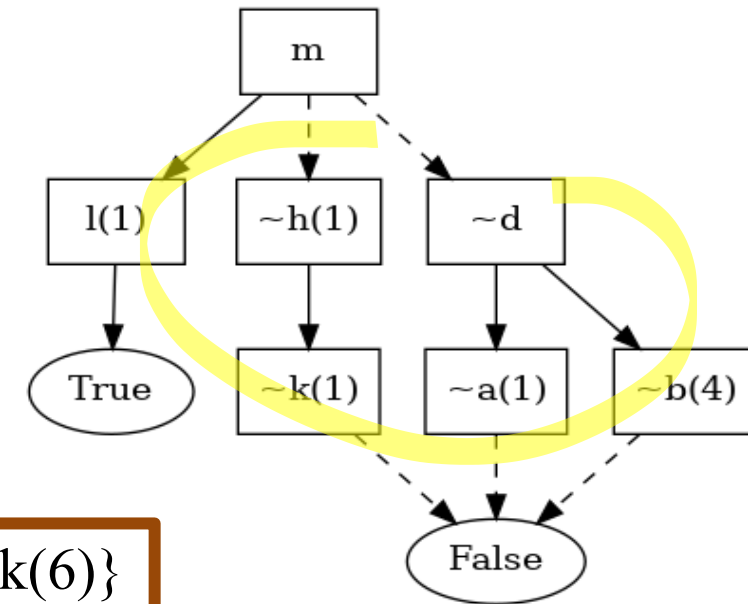
- **Task 1**: given  $\Pi \models^c a$  and answer set  $S$ , why is  $a \in S$  (or  $a \notin S$ )?
- **Task 2**:  $\Pi \otimes \varepsilon$ : how to update?

# Computing Explanation

Given an ASP program  $\Pi$ , an atom  $a$ , an answer set  $S$ .  
Compute an explanation for  $a$  being in (or not in)  $S$ .

```
(r1) m :- l(X), not d, not h(X).  
(r2) d :- b(X), a(X).  
(r3) h(X) :- k(X), p.  
(r4) b(1).  
(r5) a(4).  
(r6) l(1).  
(r7) k(6).
```

$A = \{l(1), m, a(4), b(1), k(6)\}$



Several system ICLP21/LPNMR22

Newest system considers almost all syntactic constructors of modern ASP solver

(Alviano et al. ICLP 2023)

# Computing $\Pi \otimes \varepsilon$ ? Intuition

$$\pi = \{a \leftarrow\}$$

$$(b, \varepsilon = (\{b \leftarrow a\}, \emptyset))$$

$$\pi \otimes \varepsilon = \{a \leftarrow; b \leftarrow a\}$$

$$\pi = \{\cancel{a \leftarrow}\}$$

$$(b, \varepsilon = (\{b \leftarrow \text{not } a\}, \emptyset))$$

$$\pi \otimes \varepsilon = \{b \leftarrow \text{not } a\}$$

$$\pi = \{\cancel{c \leftarrow \text{not } c}\}$$

$$(b, \varepsilon = (\{b \leftarrow \text{not } a\}, \{c \leftarrow \text{not } c\}))$$

$$\pi \otimes \varepsilon = \{b \leftarrow \text{not } a\}$$

What to keep and what to remove?

# A Proposal for Update Operator

For a set  $I$  of atoms and a set of rule  $\epsilon^+$  (w.r.t some program  $\pi_a$ ), the *residual* of  $\pi$  with respect to  $\epsilon^+$  and  $I$ ,  $\otimes(\pi, \epsilon^+, I) \subseteq \pi \setminus \epsilon^+$ , such that for each rule  $r \in \otimes(\pi, \epsilon^+, I)$ :

- $\text{head}(r) \in I$  and  $\text{neg}(r) \cap I = \emptyset$ ; or
- $\text{neg}(r) \cap \text{heads}(\epsilon^+) \neq \emptyset$ ; or
- $\text{pos}(r) \setminus I \neq \emptyset$ .

Define:  $\epsilon^-[\epsilon^+, I, \pi] =_{\text{def}} \pi \setminus \otimes(\pi, \epsilon^+, I)$

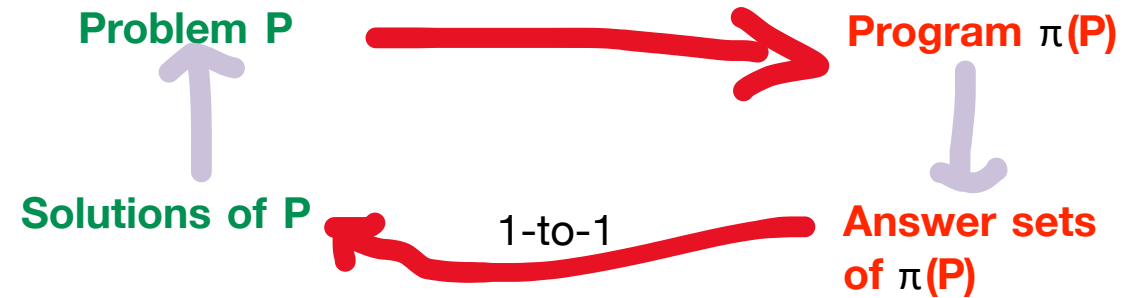
If  $\epsilon^+$  is a justification for  $q$  then  $(\epsilon^+, \epsilon^-[\epsilon^+, I, \pi])$  is an explanation for  $q$  w.r.t.  $\pi$  (i.e.,  $\pi \setminus \epsilon^-[\epsilon^+, I, \pi] \cup \epsilon^+ \models q$ )

👉  $\epsilon^-$  can be determined given  $\epsilon^+, I, \pi$

ASP implementation (*JELIA 2021*)

# MRP and Its Applications in ASP

- P encoded as a set of facts FA
  - **planning**: the domain, the initial state, and the goal are encoded as a set of facts
  - **scheduling**: the set of tasks and constraints
  - **graph coloring**: the set of nodes and edges



- $\pi(P) = FA \cup R(FA)$

- **planning**: domain independent rules for reasoning about actions' executability and effects, etc.
  - **scheduling**: rules for assigning tasks to resource and time and checking satisfiability of solutions
  - **graph coloring**: rules for assigning colors to nodes and checking satisfiability of solutions
- $R(FA)$ : obtained from grounding domain independent rules using ground terms in FA

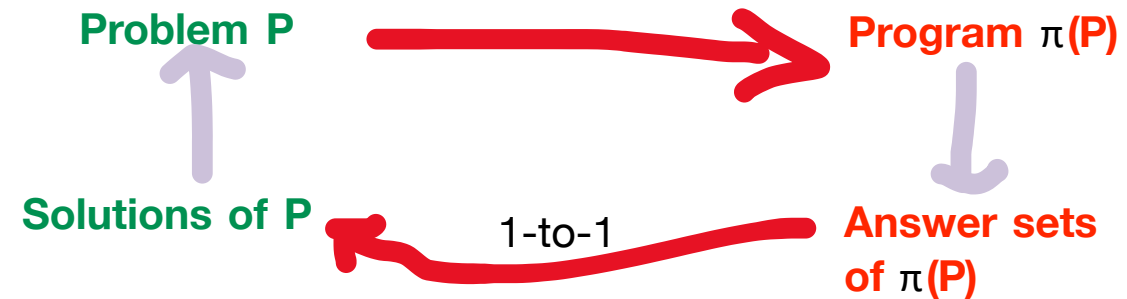
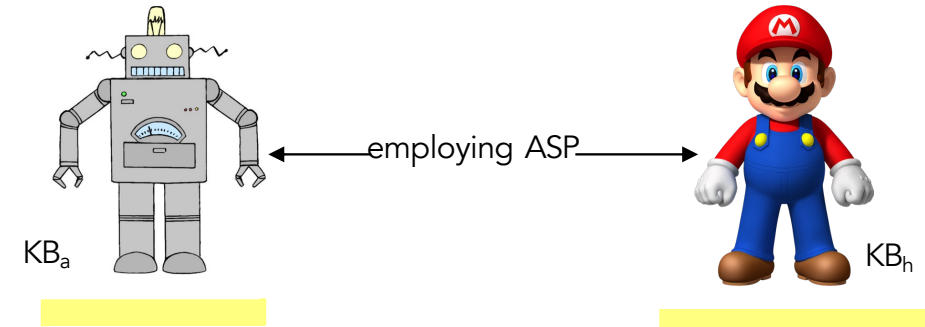


# MRP and Its Applications in ASP

When robot and human employ ASP for problem solving and

- they share the set of domain independent rules
- MRP between  $KB_a$  ( $\pi(P_a)$ ) and  $KB_h$  ( $\pi(P_h)$ ) reduces to MRP between  $P_h$  and  $P_a$

- Planning
- Scheduling
- Graph coloring
- ...



General algorithm for ASP is applicable but scalability is an issue.

# Related Work

- ❑ Earlier problems such as logic program update, diagnosis, or explanation in abductive logic programs could be viewed as instances of MRP – **one shot explanation**
- ❑ Multiagent diagnosis
- ❑ Negotiation
- ❑ Dialog

# Logic programming update

$P \otimes \phi$ :  $\phi$  is **new** information and needs to be integrated to  $P$

$\phi$  must be true in  $P \otimes \phi$ , maintaining as much information from  $P$  as possible. focus: how to construct  $P \otimes \phi$

Update obeys belief revision principles (*causal rejection principle* or *program transformation*)

- ❑ individual rules might change
- ❑  $P \otimes \phi$  might be inconsistent
- ❑  $P \otimes \phi$  might be a set of programs

**Instance of MRP:**  $(\phi, P, \phi)$ :  $P = \pi_h, \pi_a = \phi$

# Explanation in Abductive Logic Programs

Given  $(P, A)$  and a query  $q$ .

Identify a pair of hypotheses  $(E, F)$  that explains  $q$ :

$(P \setminus F) \cup E$  is consistent

$E \subseteq A \setminus P$  and  $F \subseteq A \cap P$

$(P \setminus F) \cup E \models q$

**Instance of MRP:**  $(A, P, q): P = \pi_h, A = \pi_h \cup \pi_a, \pi_a \models q$ .

# Diagnosis

Given a theory  $KB$ , a set of observations  $OBS$ , a set of predefined atoms  $AB(C)$  such that  $KB \cup OBS \cup AB(C)$  is inconsistent.

Identify a set  $D \subseteq AB(C)$  such that  $KB \cup OBS \cup (AB(C) \setminus D) \cup \neg D$  is consistent.

**Instance of MRP:**  $(\neg AB(C), KB \cup OBS \cup AB(C), \text{True})$

# Summary & Outlook

- ❑ Model reconciliation for explainable planning
  - ❑ One-shot explanation
  - ❑ Dialog for explanation
- ❑ Logic based formalization of MRP
  - ❑ Characterizations of explanation of MRP
  - ❑ Method for computing explanation of MLP using ASP
- ❑ Future work
  - ❑ Multiagent diagnosis
  - ❑ Negotiation
  - ❑ Dialog

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